ALMA Memo. No. 477

Notes on Axis Intersection for MMA Antennas

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1 Introduction

This memo incorporates some notes I wrote down on 1998-Dec-10 when Peter Napier asked me to look into the problem of specifying the axis intersection quantities (two angles and a separation) for the MMA antennas. I provide no further information than what is directly in the notes, but it seemed that the information therein should be retained historically, so I've made this electronic version.

Some notes on azimuth & elevation axis non-intersection for MMA

much of this is based on Cam Wade's memo (VLA Test Memo * 104)

first, what if angles are not precisely 90°? I've drawn on Cam's figure 1 the angles that we are specifying for MMA antennas (0, & 02).

If Oz ≠ 90°, this simply mimics an azimuth pointing offset, and can be handled as such, I think.

If 0, ≠ 90°, this changes the vector D which connects P to P' (see figure). If we let 0, = 90°-4, and assume 4 is small so that cos 4-1 and sin 4-4, then,

$$D = \begin{cases} (a-b \sin h) \cos Z + (c-b\Psi) \sin Z \\ -(c-b\Psi) \cos Z + (a-b \sinh) \sin Z \\ c\Psi + b \cosh \end{cases}$$

this adds some terms (involving by & c7) to the fringe phase error;

 $\Delta \phi = \alpha \cosh - \Delta h (\alpha \sinh - \beta) - \gamma \Delta z \cosh + \Delta \phi_{\Theta}$

the sope are the additional terms:

ΔΦo = βYDh cosh + TY (sinh + Dh cosh)

= Yahcosh (B+x) + & Ysinh

assuming 4 is small, Do is negligibly small

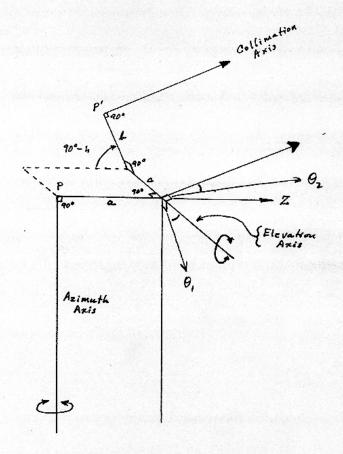


Figure 1 from Wade 1974

Now, what if we make no attempt to measure a, b, and c on the antennas, and rely on our secondary calibrator to account for \$\Delta\phi\$?

in the simplest case, assume that at t=0, we measure phase on a calibrator at elevation he, then after some interval Dt, we measure it again (at elevation he,). if we use simple linear interpolation of these measured phases, and apply them to the source visibilities, we get an error like:

 $\Delta \phi_{k}(t) = \alpha \cos \left[h_{s}(t)\right] - \phi_{e}(t)$ $= \alpha \left\{\cos \left[h_{s}(t)\right] - \left[\cos h_{e_{s}} + \frac{\cos h_{e_{s}} - \cosh_{e_{s}}}{\Delta t} \cdot t\right]\right\}$

i.e., there is some error due to the calibrator not being at the same elevation as the source, and some due to approximating a cosine by a linear interpolation.

(as long as ∆t is relatively small (≤ 30 mins) the error due to the different source and calibrator elevations dominates. in this case,

| Adk | max & of &h Sin hour

where Sh is the elevation difference between source & calibrator.

what to use formed ha?

based on Bob Brown's noise temps (in his SPIE paper), and Scott Foster's derived distances to calibrators at 90 GHz (MMA memo 124), and a scaling for source number counts which goes like:

constraint (of same order anyway)

tess the variation of elevation due to uses phase to go through 3. If turn, min - 7.5 deg, so about same c derived on next, page...

N, 0 S, -1.5 V 3.5

(see Kitayama et al. for S, scaling, and Franceschini et al. for & scaling)

and assume you need 100 per baseline in a 1 min calibration scan, then you might have the following:

V (GHz)	Sh (deg)
115	1,5
230	0-6
345	0.4
410	0.4
675	0.6

this is for 90% of sources...

these numbers seem a bit small. let's assume that sh might be as large as 3 deg. let us also assume that we want 1200

nde that this (18 turns). then: fundamentally

limits

18 2 a . 0.052 astrometry...

(this error, if left

→ X 5 1.1

unaccouted for)

MMA's Shortest wavelength (850 GHz)

- 1~350 µm, so

accuracy of a \$ 200 µm

REMEMBER THAT THIS IS ONLY NEEDED IF acosh IS NOT MEASURED CALIBRATED

what if we measure/calibrate the x cosh term, but ignore the rest?

NOTE: this is what the VLA doesthis is the so-called k-term correction.

It is measured every year or so, when in C or D-config, and is usually quite stable over time. The measurement of x (a) is made possible by being able to go OTT. This makes x (a) easily distinguishable from other baseline/pointing terms.

in this case, the residual phase is:

DO" = - a Dh sinh + BAh - DAZ cosh

use this to constrain a, b & c separately ...

Ada = - & Ah sinh

let hago sinh -> 1

100 = x sh

 $\alpha = a/\lambda$, and let Δh be some multiple of HPBN ($\Delta h = n\lambda/D$), then

100" ~ an/D

let D=10 m and $|\Delta \phi_a^*| \lesssim 20^\circ (\frac{1}{18} turns) \frac{\pi}{3} rad)$ and $n \sim 10$, then

accuracy of a & 3 cm

Similar constraint for b & c, so this is unimportant ... (relatively)

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what about decorrelation due to acosh term?

even if you correct for ocosh, you have to worry about how much it changes over an integration cycle. the change in ocosh over 1 integration is roughly:

1 (xcosh) ~ x sh

with the elevation change given by:

Sh ~ 2 T st rad

for integration time At sec. if we want the error over an integration cycle to be less than 20 deg, then,

d x 2π Δt < 20 86 400 ~ 360

Da < 760 turns

at 350 mm, this corresponds to:

accuracy of a & 130 mm e.g. @ Dt = 10 sec, occuracy of a & 1,3 cm

if this is not satisfied, given eventual values for a and At, then we may need a 2nd order a cosh correction (provide a cosh and a acosh to fringe frequency

calculator - this is how VLA-PT will be done).

Tother vefos: Wade, Apt, 162, 381 Sovers et al., Rev. Mad. Phys, 70, 1393