

Grazing reflection from  
Woods "Physical Optics", page 40

Path difference is  $2H \cos \theta$  where  $H$  is vertical height of bump and  $\theta$  is angle between ray and vertical. This applies to all angles of  $\theta$ .

Let  $\theta = 0$ . Assume a surface which has random roughness with mean values as given. Then the mirror efficiencies will be approximately (estimates only)

$H$	$\epsilon$
$\frac{1}{4} \lambda$	50
$\frac{1}{8} \lambda$	80
$\frac{1}{16} \lambda$	95
$\frac{1}{32} \lambda$	99

When  $\theta = \theta$  the value of  $H$  for same efficiency must be divided by  $\cos \theta$  or

$\epsilon$	$H$
50	$\lambda / (4 \cos \theta)$
80	$\lambda / (8 \cos \theta)$
95	$\lambda / (16 \cos \theta)$
99	$\lambda / (32 \cos \theta)$

Thus as  $\cos \theta$  approaches  $90^\circ$ , or grazing incidence, the value of  $H$  may be very large and still have excellent efficiency

## Reflection Coefficient & Roughness.

"Reflection & Absorption of 9cm Waves", L.H. Ford and R. Oliver, Proc. Phys. Soc. (London), Vol 58, May 1946, p 265-280.

Specular Reflection will occur if

$$H \cos \theta \ll \lambda \quad \text{where}$$

$H$  is average height of irregularities

$\theta$  is angle of incidence (angle to vertical)

$\lambda$  is wavelength.

When  $H \cos \theta / \lambda$  is about  $1/5$ , the coefficient of reflection is 0.5 approx.

When  $H \cos \theta / \lambda$  is about  $1/2$ , the coefficient of reflection is improbably as large as 0.1.

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also see "Radio Wave Propagation" by Burrows and Attwood, Academic Press 1949,

# The Reflection and Absorption of Radiation at 9 cm Wavelength.

by L. H. Ford & R. Oliver,  
Proceedings of the Physical Society  
1st May, 1946, Vol 58, Part 3, No 327, p 265-280

Abstract from conclusions on pages 278 & 279

- (3) The change in phase on reflection is about  $180^\circ$  for vertical polarization at angles of incidence appreciably greater than Brewster's angle, and negligible at angles of incidence appreciably less than Brewster's angle.
- (4) The change in phase on reflection is about  $180^\circ$  for horizontal polarization at all angles of incidence.
- (9) The depth of the surface irregularities multiplied by the cosine of the angle of incidence must be a small fraction of the wavelength. When this fraction is about  $\frac{1}{5}$ , the reflected ray may be reduced to about  $\frac{1}{2}$  its proper value, and when the fraction is  $\frac{1}{2}$  a reflection coefficient greater than 0.1 is improbable.

M. I T report # 664 by Van Vleck

"Atmospheric Absorption of Microwaves"

Figure 3 gives .01 DB/nautical mile at 25 cm

$$\frac{\Delta\nu}{c} = .02 \text{ cm}^{-1} \quad \frac{\Delta\nu}{c} = 0.5 \text{ cm}^{-1}$$

Published in Physical Review

April 1st, 1947 Vol 71, page 413-433



10-6-49

Since the wave trains which create the interference are of finite length it is obvious that if the path difference is greater than the length of the train no interference can occur. The various lobes in pattern are similar to orders in a grating. By using very large orders or high lobes some information may be had upon the actual length of wave train. Likely a collector with poor resolving power will be needed for this experiment so that it can look high up and low down at same time.

Visit to Evans Laboratory March 10th 1950.

Talked to Blackwell and Crenshaw at some length. They thought the variation in intensity from pulse to pulse was probably due to apparatus difficulties. This was due to fact the oscillator didn't come up on exactly the same frequency each time. The narrow pass band of 50 cps would exclude some pulses. Furthermore, to get the results they did have, it was necessary to manipulate the tuning every few minutes. Some days this trouble was very bad and no echoes were secured. There was no obvious difference in the randomness of the echoes secured over water to the east or land to the west. Therefore it was concluded that there was no appreciable duct phenomena over the sea. Likewise there was no obvious difference between summer and winter. Data was secured intermittently from Jan 1946 thru Nov. 1947. Echoes over land to west were always weaker due to poor reflection coefficient of land. The lobe structure was also poorly defined and phenomena seemed to be approaching free space transmission. They thought some scintillation might occur but it could not be detected due to above trouble with the apparatus.

(over)

Scintillation is due to fact that light ray is bent by atmospheric refraction in a random manner. Since the aperture of your eye is small the ray may move out of the aperture at times. This will cause the image to tremble. Conversely, the aperture of a telescope is large. Thus the ray will always be present but merely move around over the aperture. This will cause the image to dance.

Please get copies of following  
publications from the Navy Hydrographic  
office at Suitland, Md.

"Wind, Sea & Swells; Theory in Forecasting"  
# H0601

"Wind, Waves & Swells; Principles & Forecasting"  
H011275

"Breakers & Surf" H0234

Grote Reber

3-13-50

Hydrographic office <sup>to</sup> G153  
Switland Md.  
Sea & Swell charts

H0601 Wind Sea & Swells <sup>1947</sup> 50¢  
Theory of Relation in  
Forecasting

✓ H0602 Wind Waves at Sea, \$2.80  
Breakers & Surf 1947

H011275 Wind Waves & Swells 40¢  
Principles & Forecasting 1944

Switland, Md.

Div. of Distribution X12

H0234 Breakers & Surf <sup>1944</sup> 40¢

~~code X12~~  
~~Talk to Division of Oceanography, The U.S. Navy~~

calm, low, med & high.  
0-1ft 1-3ft 3-8ft 8-up.

✓ North East Pac. HO-10,712-D  
Sea & Swell Atlas.

Mr. Bates  
Division of Oceanography

9/14/48

U.S. Hydrographic office

HO-602 - Wind waves & sea, breakers

& surf - 1947 (2.80)

HO-10,712 - II - Sea & swell atlas of  
northeast Pacific

HO 9-15-48

HO code 153

ext. 12

Div. of Distribution

rec'd 9-24-48

Reber

501



5-25-50

Talked to Ament at NRL for 20 minutes  
He is on G 130 x 172. He said during  
May 1946 they made various experiments  
off the northeast coast of Oahu. The  
receiver was on a tower 106 feet high above sea,  
with other receivers at 50, 30 and 15 feet. The  
transmitter was in an airplane which height  
varied from 400 to 1000 feet. The propagation  
was in a direction from N.E. to S.W. a north  
east wind was blowing 8 to 10 knots so they were  
propagating off the backs of the waves. For  
this type of one way experiment where reciprocity  
exists the direction into or with the wind  
makes no difference. However for radar work  
considerably less back scatter is obtained when  
working to backs of waves.

at 10 cm the first six lobes showed ratios  
of maxima to minima of 13 to 20 DB, at 3 cm  
the ratio was 6 to 8 DB.

a 10 knot wind on a 1000 mile fetch will  
raise waves more than a foot high.

apparently some 700mc experiments were made eastward from the Annex station across Chesapeake Bay. They got quite a spray of points, when the reflection coefficient was computed, even at this frequency. There are some MIT reports describing results at Sand X band.

If the earth were flat the angular distance between maxima would be

$$\Delta \alpha = \sin^{-1} \frac{\lambda}{2h}$$

Where  $\lambda = 25 \text{ cm}$  and  $h = 250 \text{ ft} = 7610 \text{ cm}$

$$\frac{\lambda}{2h} = \frac{25}{2 \cdot 7610} = 1.642 \times 10^{-3} \text{ radian}$$

$$\Delta \alpha = 57.3 \times 1.642 \times 10^{-3} \times 60 = 5.65 \text{ minutes of arc.}$$

If the source were as large as 3 minutes of arc the interference lobes would be swamped out and an effect such as Piddington describes would result.

Since the frequency is so high the ionosphere cannot have any effect. However the lower atmosphere may have humidity gradients which could be very rough and rapidly changing. These would break up the interference pattern in the manner described. Furthermore, they would be more pronounced at 25 cm than at 100 mc. The effect is aggravated by operating from the shore of a hot continent.

A combination of these two effects probably explains Piddington's trouble and not oxygen or roughness of the sea.

Sunset at Atua

9-9+10-50

3 cm and 10 cm apparatus both using mirrors 6 feet in diameter were operated on Alexai Point. They were about 30 feet above sea level. The sun set behind some mountains at the base of Murder Point and across Massacre Bay. These mountains were about 1500 feet high and about 7 miles away. Their apparent angle above the horizon was thus about  $2\frac{1}{2}$  degrees.

When the sun set behind the mountains, a good interference pattern was secured at 10 cm but not at 3 cm or at 0.8 cm which used a mirror 2 feet in diameter. The apparatus was on a polar axis which kept the mirror pointed at the center of the sun. For an interference pattern to occur, two waves must be present. Since both waves must originate in the sun and come over the tops of the mountains at  $2\frac{1}{2}^\circ$  above the sea, the reflected wave from the sea will make an angle of  $5^\circ$  or more with the direct wave at the receiver. Since the mirror is kept pointed at the direct wave, the reflected wave will be  $5^\circ$  or more off axis. This will cause the reflected wave to be considerably attenuated and reduce the amplitude of the interference pattern. At 10 cm the beam is about  $3\frac{1}{3}^\circ$  wide at 3 dB down. Thus it is probably about 8 dB down at  $5^\circ$  off center. Even with this attenuated reflected wave a decent interference

pattern is secured (about 30% amplitude change).  
At 3 cm the circumstances are much less favorable. The beam is about  $1^\circ$  wide at 3 dB down. Thus it is probably over 20 dB down  $5^\circ$  off center. This extremely weak reflected wave will not be sufficient to create a good interference pattern, and the sun will simply dip out gradually as it is obscured by the hills. This is what was observed with a very faint (less than 10%) ripple as an interference pattern.

The sea in Massacre Bay had a swell of about 2 feet with waves a foot or more high and a few white caps. It was quite choppy. Apparently even so rough a sea is a good reflector at 10 cm wavelength.

12-19-50

Later calculations showed the reflections were from steel matting at a distance of about 6 feet below mirror instead of sea at 30 feet below mirror. This was determined by measuring the period of oscillation and computing rate at which sun set. The geometry also showed that Massace Mountain's cut off sun as a straight edge before an angle small enough to reach the sea was secured.



January 10, 1952

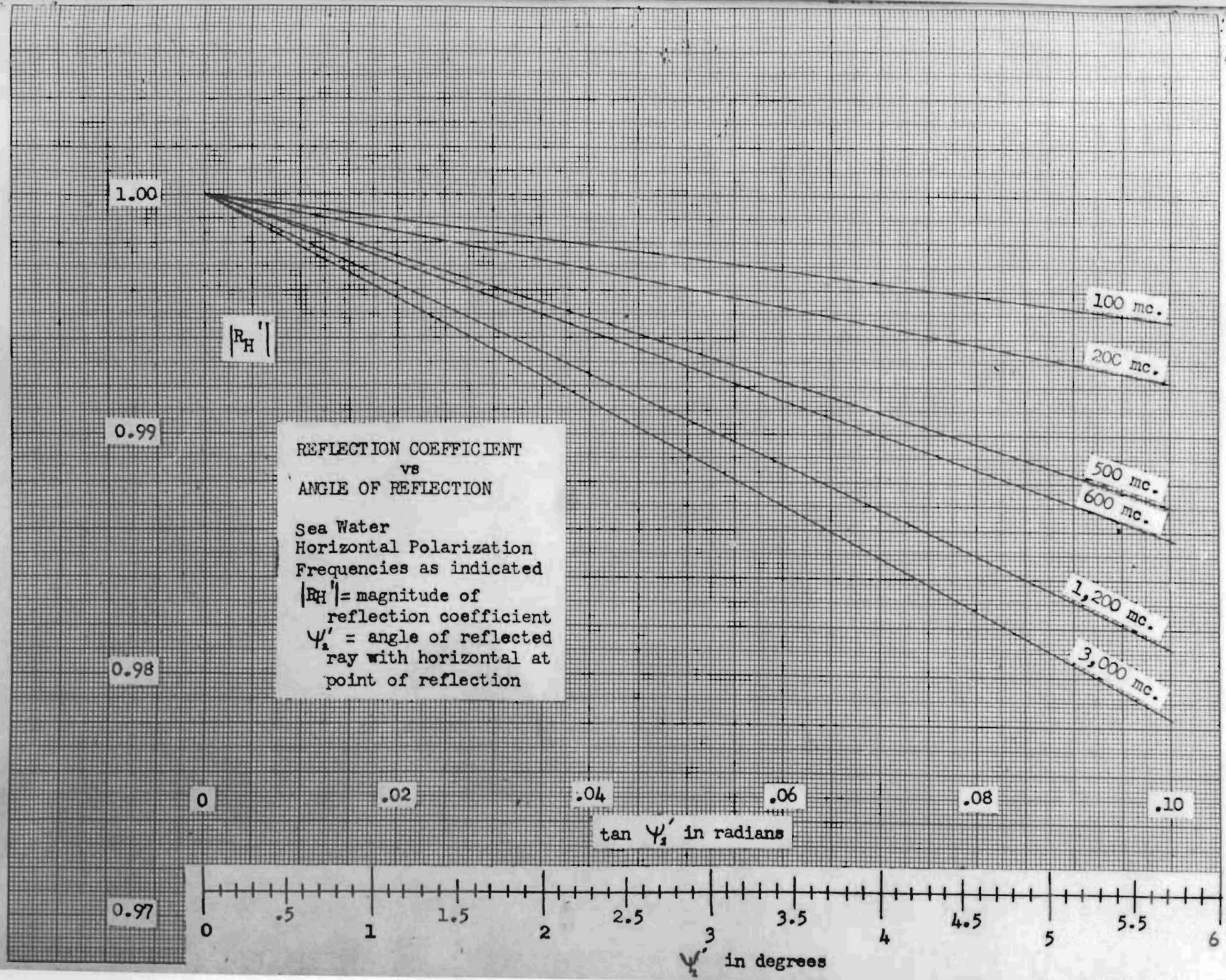
Visited Library of Congress. They don't have H.O. Misc # 11,117 "Waves in the North Pacific Ocean". However I found an old card dated about 1878 filed under Hydrographic which was entitled "Waves in North Pacific Ocean". This is different from former as it contains histograms for 1929-1938.



These are from Radiation Lab  
Report C-11 dated Sept 22, 1943  
by Hutner, Dodson, Gill, Parker  
and Howard. The title is  
"Field Intensity Formulas"

Bureau of Standards Library  
Number 23 dated Oct 18, 1946

Note: Brewster angle is proportional to  $(\text{wavelength})^{-1/2}$  or  
 $\theta = k/(\lambda)^{1/2}$ . When  $\lambda$  is in meters and  $\theta$  in degrees,  $k = 3.5$  for  
200 m $\mu$  and below;  $k = 3.4$  for 500 m $\mu$ ,  $k = 2.0$  for 3000 m $\mu$ .



REFLECTION COEFFICIENT  
vs  
ANGLE OF REFLECTION

Sea Water  
Horizontal Polarization  
Frequencies as indicated

$|R_H'|$  = magnitude of  
reflection coefficient  
 $\psi'$  = angle of reflected  
ray with horizontal at  
point of reflection

FIG. 5.1



REFLECTION COEFFICIENT  
 $R_v$   
 ANGLE OF REFLECTION

Sea Water  
 Vertical Polarization  
 Frequencies as Indicated  
 $R_v$  - magnitude of  
 reflection coefficient  
 $\psi_r$  - angle of reflected  
 ray with horizontal

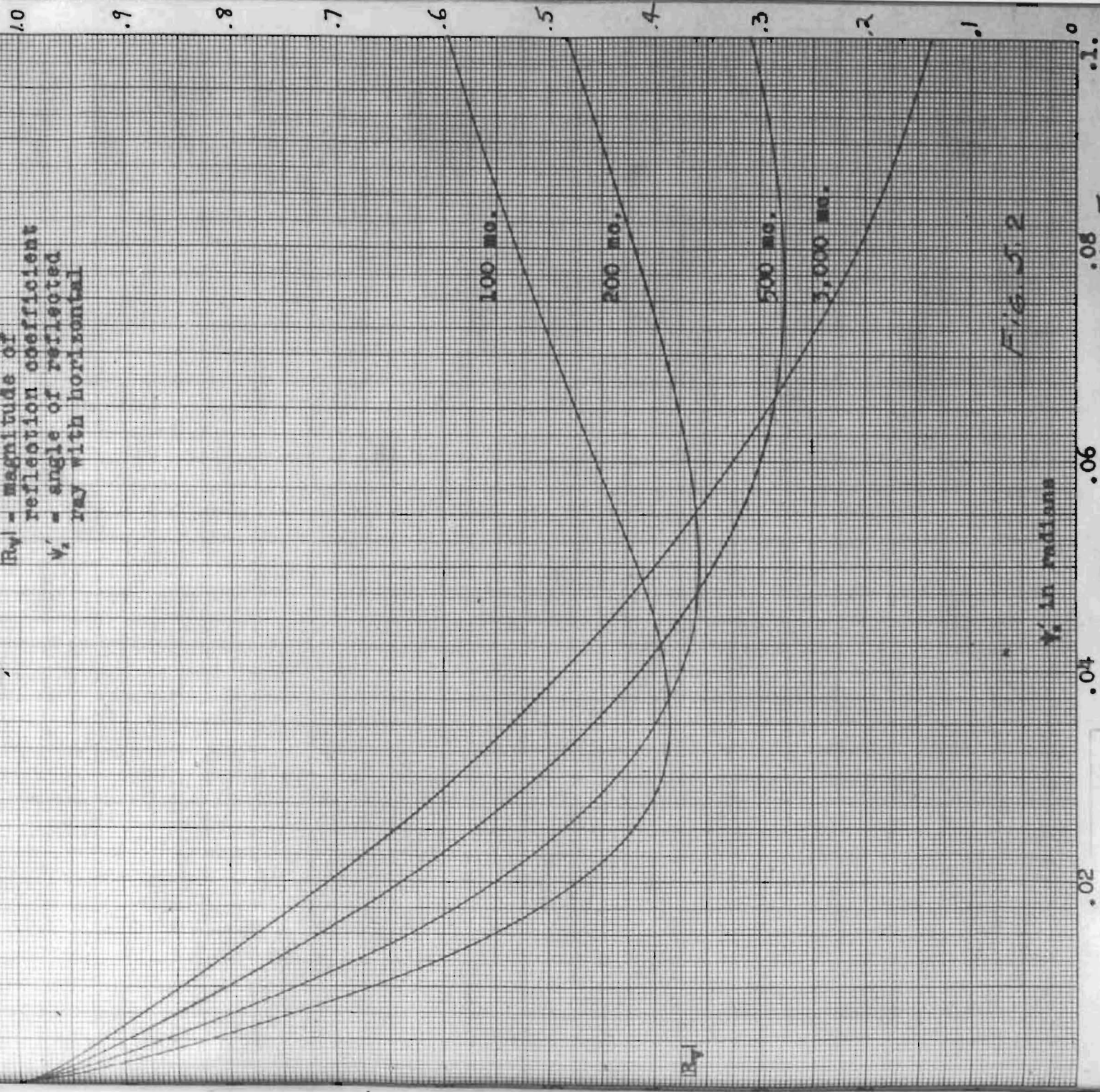
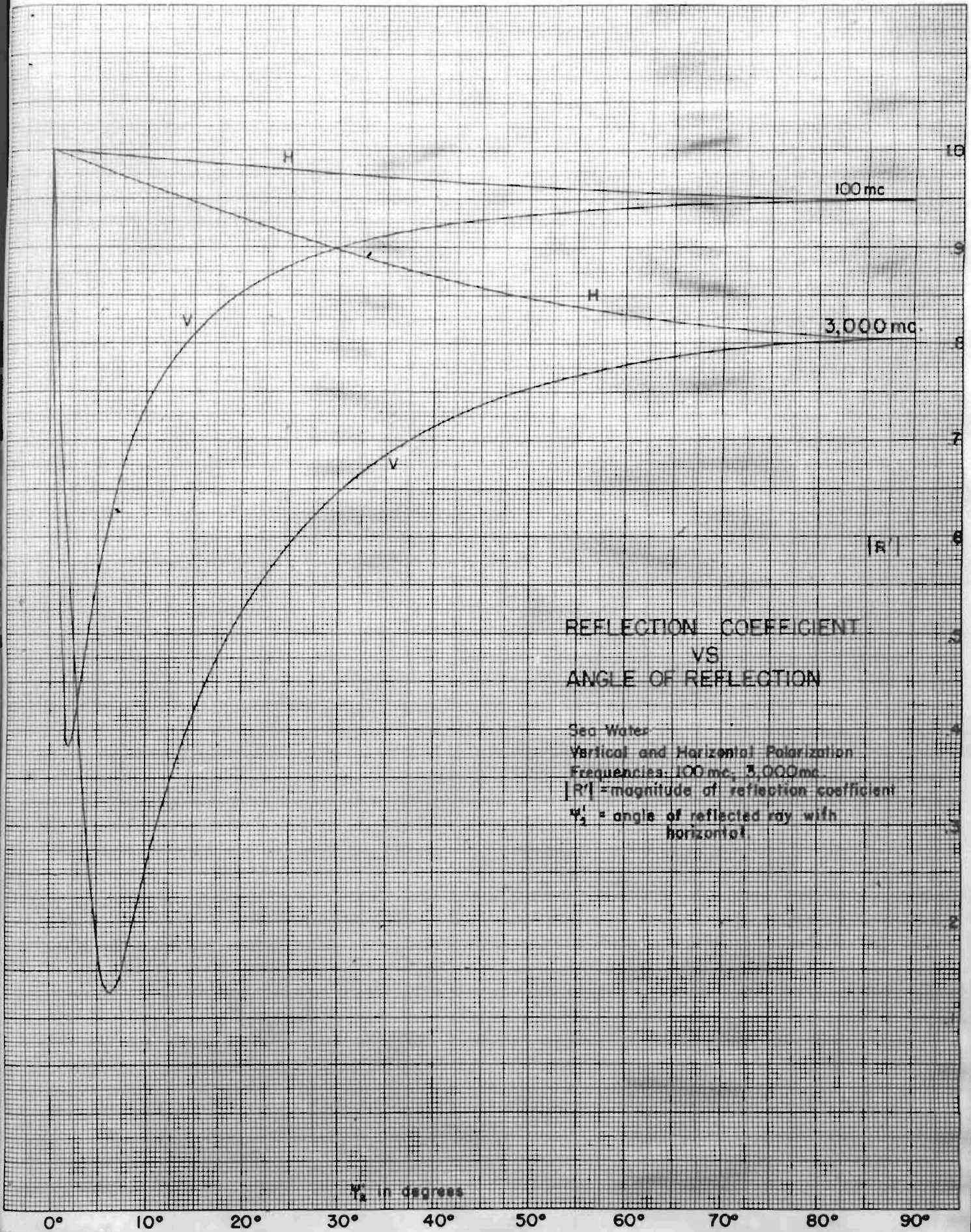


Fig. 5.2

$\psi_r$  in radians

FIGURE 5.3



REFLECTION COEFFICIENT  
VS  
ANGLE OF REFLECTION

Sea Water  
Vertical and Horizontal Polarization  
Frequencies: 100 mc, 3,000 mc.  
 $|R'|$  = magnitude of reflection coefficient  
 $\theta_2$  = angle of reflected ray with  
horizontal



PHASE OF REFLECTION COEFFICIENT  
vs  
ANGLE OF REFLECTION

Sea Water  
Vertical Polarization  
Frequencies as indicated  
 $\phi_r$  = phase of reflection coefficient:  
 $\psi_r$  = angle of reflected ray with horizontal

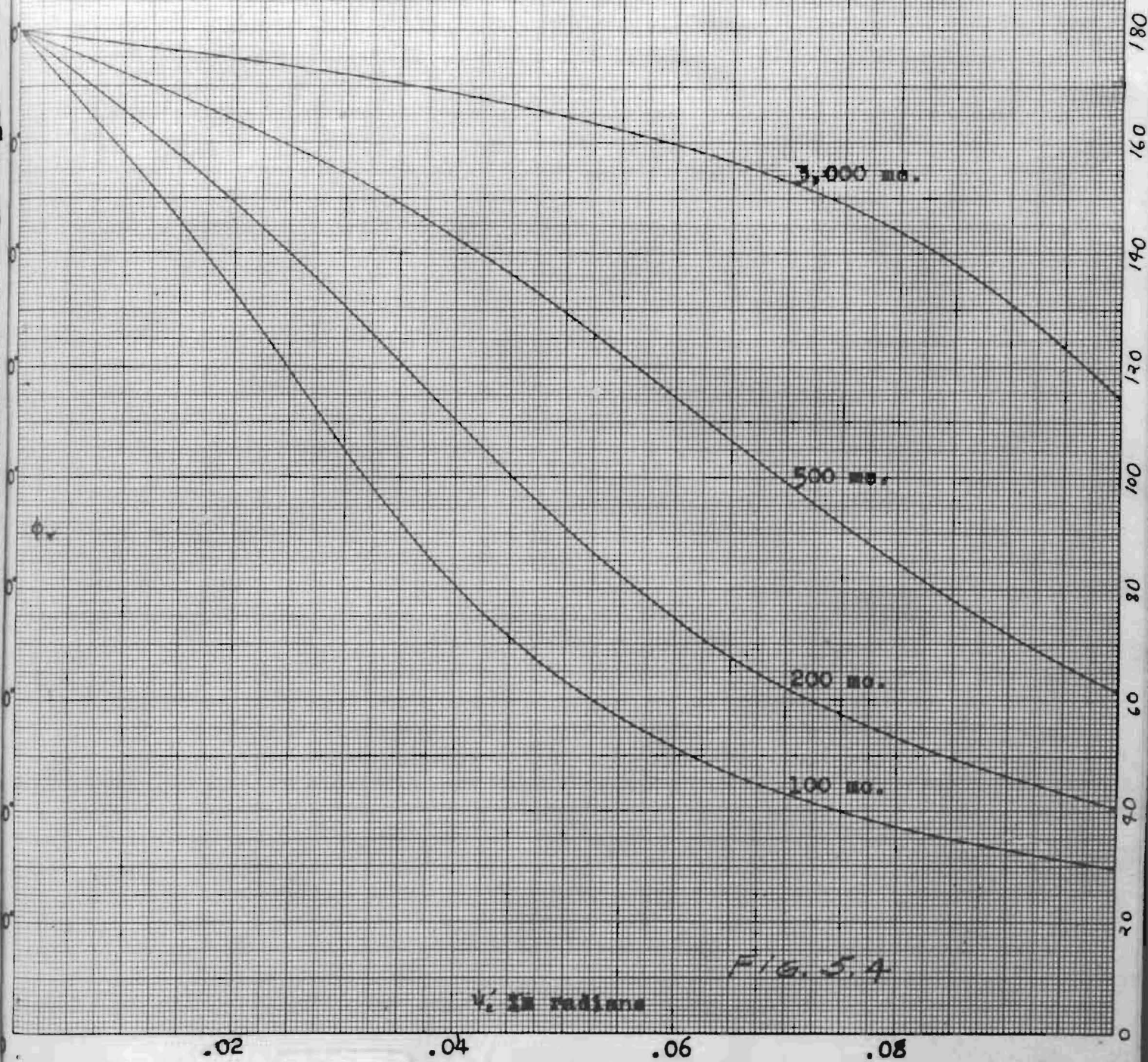
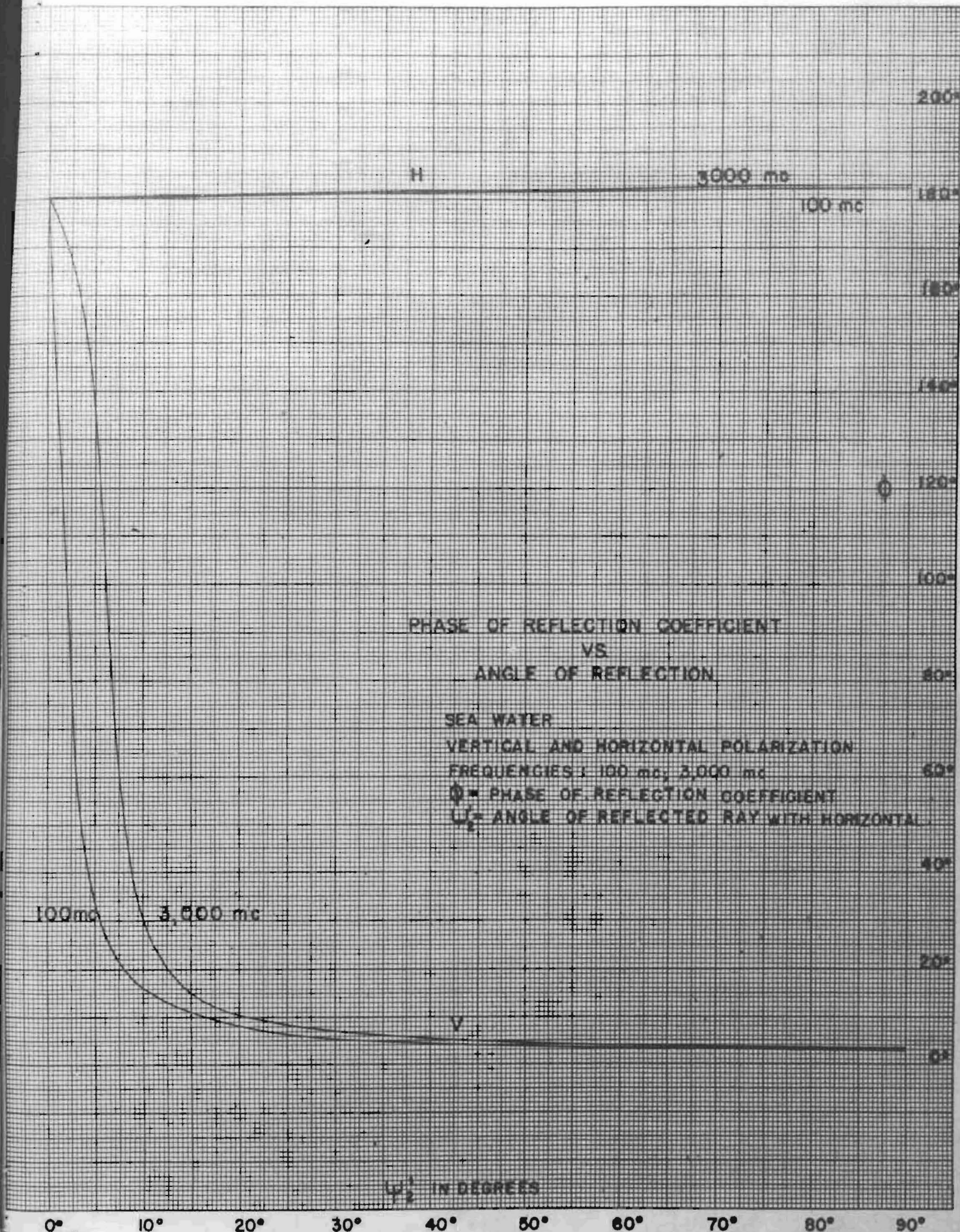


FIG. 5.4

$\psi_r$  in radians



FIG. 5.5



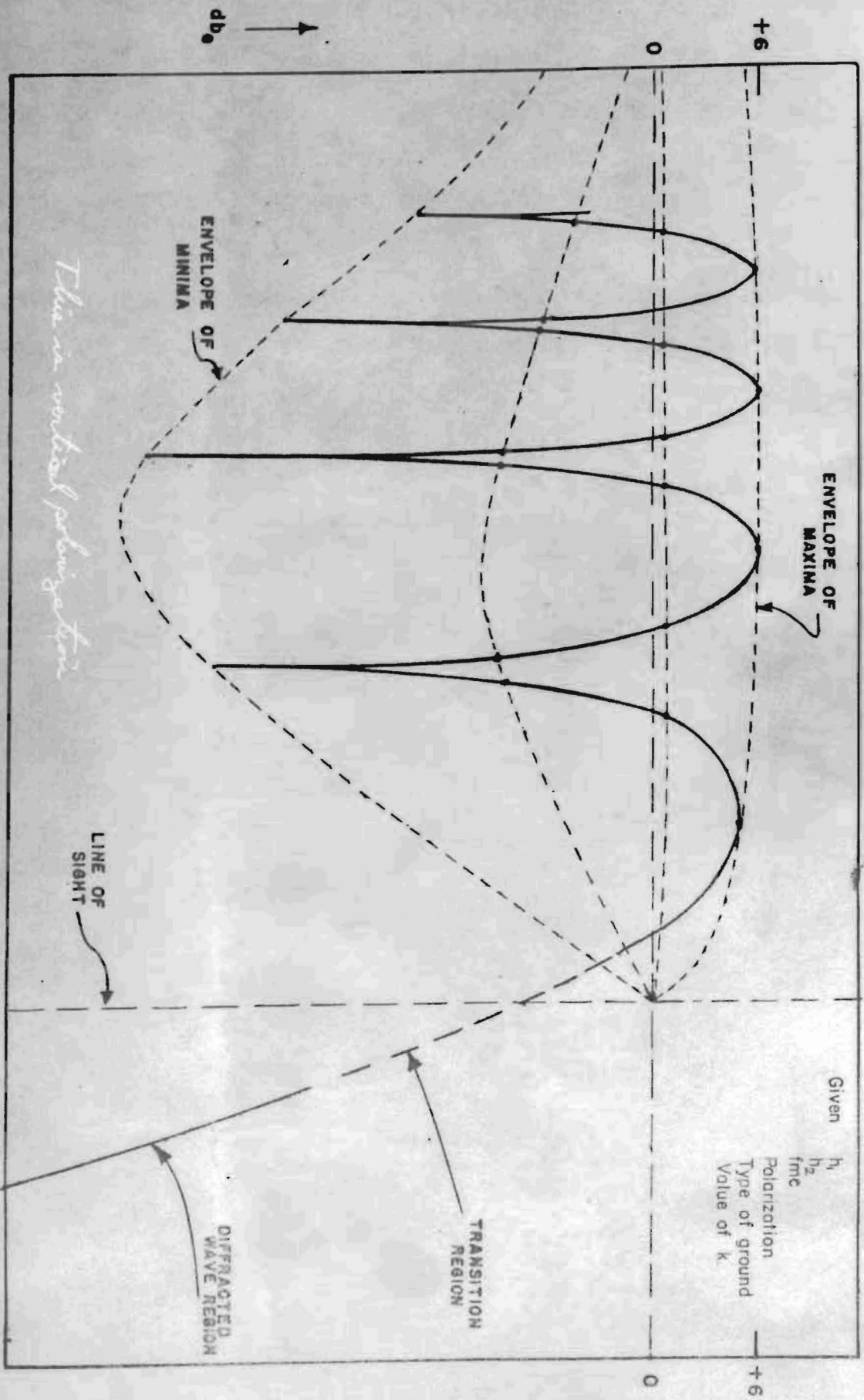


FIG. 71

REPORT C-11

$d$  (LOG SCALE)

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