Tunnel Transit-Time (TUNNETT) Devices for Terahertz Sources*

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Abstract

The potential and capabilities of Tunnel Transit-Time (TUNNETT) Devices for power generation in the 100–1000 GHz range are presented. The basic properties of these devices and the important material parameters which determine their properties are discussed and criteria for designing such devices are presented. It is shown from a first order model, that significant amounts of power can be obtained in this frequency range.

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1. Introduction

Two-terminal transit-time devices such as IMPATTS are capable of generating significant amounts of power at high-frequencies [1–3]. However, because of the avalanche process, they are very noisy and their efficiency decreases significantly at extremely high frequencies. Also, because of the very narrow drift regions and high doping densities required at such high frequencies, tunneling mechanisms become dominant and effect the performance. Through proper design of the device, we can take advantage of the very fast tunneling process to obtain extremely high frequency and reduce the noise. Such devices have been considered previously [4–7] and preliminary experimental results have been obtained in the 100–300 GHz range. Recent advances in material growth and processing technology will make a significant impact on further development of such devices.

In this paper, the basic principles of two-terminal transit-time devices will be presented and the differences among the various charge injection mechanisms will be discussed. This is followed by an assessment of the R.F. power generation capability of TUNNETTS as well as device design for various operating frequencies.

2. Basic Principles of Two-Terminal Negative Resistance Transit Time Devices

Two-terminal transit time negative resistance devices generally consist of a charge injection region and a drift region as shown in fig. 1. There are several means of injecting the charge $Q$ into the drift region. These include:

![Diagram of Two-Terminal Negative Resistance Transit-Time Device](image-url)
a) Thermionic Emission Over a Barrier (BARRITT):
   This can be realized from a forward-biased p⁺- n or n⁺- p junction or by
   incorporating a wide band semiconductor layer to form a heterojunction barrier.

b) Tunneling Through a Barrier (TUNNETT):
   This can be realized by tunneling through a single heterojunction barrier, resonant
   tunneling through a double barrier [8,9] or tunneling in a reverse-based p⁺- n⁺
   junction.

c) Avalanche Multiplication (IMPATT):
   This is realized through avalanche breakdown.

d) Mixed Tunneling or Thermionic Emission and Avalanche Multiplication (MITATT):
   This results when two types of mechanisms are involved in the charge generation.

When a pulse of charge of $Q$ coulombs/cm$^2$ is injected into the drift region and
travels with a velocity $v_Q$ in the drift region, the current density induced in the external
circuit is given by

$$J_{ind} = \frac{Q}{W} \left[ v_Q - \frac{W}{W} \frac{dW}{dt} \right]$$

where

$W$ = the width of the depletion layer
and $W_c$ = the location of the charge $Q$.

For the sake of simplicity and since most of the devices of interest here will be
punched through at the bias voltage, and the device is designed to maintain a high
field in the drift region, we can assume that $W$ is constant and $v_Q = v_s$, where
$v_s$ is the saturated velocity.

Under these conditions, the current voltage waveforms (under large signal conditions
which are of interest here) for all of the above devices can be represented approximately
as shown in fig. 2. In this figure,

$V_{dc}$ = the d.c. voltage (V)
$V_{RF}$ = the magnitude of the R.F. voltage (V)
$\Theta_m$ = the phase angle of charge injection (rad.)
$\Theta_w$ = the phase width of the injected charge pulse (rad.)
\[ \Theta_D = \text{the drift region transit angle (rad)} \]
\[ = \omega \tau_D = \omega W/v_s \]
\[ \tau_D = \text{the transit time through the drift region (sec.)} \]
\[ J = \text{the current density (A/cm}^2) \]

From the waveforms shown in fig. 2, it can be easily shown that the RF power density (watts/cm²) can be expressed as,

\[ P_{RF} = \frac{1}{2\pi} \int_0^{2\pi} J_{ind}(\omega t)V_{RF} \sin(\omega t) \, d(\omega t) \]  \hspace{1cm} (2)

which simplifies to

\[ P_{RF} = V_{RF} J_{dc} \left( \frac{\sin(\Theta_w/2)}{\Theta_w/2} \right) \left( \frac{\cos \Theta_M - \cos(\Theta_M + \Theta_D)}{\Theta_D} \right) \]  \hspace{1cm} (3)

The device efficiency is

\[ \eta \triangleq \frac{P_{RF}}{P_{dc}} = \left( \frac{V_{RF}}{V_{dc}} \right) \left( \frac{\sin(\Theta_w/2)}{\Theta_w/2} \right) \left( \frac{\cos \Theta_M - \cos(\Theta_M + \Theta_D)}{\Theta_D} \right) \]  \hspace{1cm} (4)

\( \Theta_M \) and \( \Theta_w \) result primarily from the device design of the generation region and this will determine the particular mode of operation.
Figure 3 Current Voltage Waveforms for the IMPATT MODE

For IMPATT mode operation, $\Theta_M \equiv \pi$ and $\eta$ becomes

$$\eta = \left(\frac{V_{RF}}{V_{dc}}\right) \left(\frac{\sin(\Theta_w/2)}{\Theta_w/2}\right) \left(\frac{\cos \Theta_D - 1}{\Theta_D}\right).$$  \hfill (5)

For maximum $\eta$ (negative for power delivery), we would like $\Theta_w$ to be as small as possible. This implies a small charge-generation region width, small voltage drop across the generation region and $V_G/V_D$ as small as possible, where $V_G$ is the voltage across the generation region and $V_D$ is the voltage across the drift region.

As an ideal case, let $\Theta_w \rightarrow 0$ (very sharp pulse). This assumption is made for simplicity since we are interested here in a first order estimation. Even if $\Theta_w$ is $\pi/2$ (which is quite wide for most cases), the estimates will be reduced by a factor of $2/\pi$ which is small relative to the estimates of interest here.

For this case we have

a. $\Theta_m \equiv \pi$ (IMPATT mode)

$$\eta = \frac{V_{RF}}{V_{dc}} \left(\frac{\cos \Theta_D - 1}{\Theta_D}\right).$$  \hfill (6)

For $\Theta_D = \pi$, $\eta = -(2/\pi)(V_{RF}/V_{dc})$, for $\Theta_D = \pi/2$, $\eta = -(2/\pi)(V_{RF}/V_{dc})$, and for $\Theta_D = 0.74\pi$, $\eta = -(2.27/\pi) \ (V_{RF}/V_{dc})$. The current voltage waveforms for these cases are illustrated in fig. 3.
It is worth noting that the d.c. voltage is directly proportional to the width of the drift region and thus to $\Theta_D$. Since the R.F. voltage is directly proportional to the d.c. voltage, then the R.F. power density will be directly proportional to $\Theta_D$. Also the capacitance of the device is inversely proportional to $\Theta_D$ (or $W$) and thus it is desirable (as will be shown later) from an impedance matching consideration to make $\Theta_D$ or $W$ as large as possible for maximizing power. Thus even though the efficiency for $\Theta_D = \pi/2$ or $\pi$ is the same, the power generation capability will be much higher for the $\Theta_D = \pi$ case.

It is also important to point out that in an actual device, $\Theta_m$ will be less than $\pi$ and thus a minimum drift angle is required before the device exhibits a negative resistance. Therefore a frequency will exist, usually referred to as the avalanche frequency $\omega a$, below which the resistance will be positive. This is desirable since it will then be easier in such a device to eliminate bias-circuit oscillations which would be difficult to suppress if the negative resistance extended all the way to d.c. Such a device will then exhibit a negative resistance (and thus is capable of oscillation) between $\omega a$ and $\omega \tau_D = 2\pi$. It will also have islands of negative resistance at higher frequencies but with much reduced power generation capability.

b. For $\Theta_m = \pi/2$ (TUNNETT, BARRITT)

$$\eta = (V_{RF}/V_{dc})(\sin \Theta_D/\Theta_D) \quad (7)$$

For $\Theta_D = (3\pi/2)$, $\eta = -(2/3\pi)(V_{RF}/V_{dc})$. The current voltage waveforms for this case are shown in fig. 4. It is seen that, compared to an IMPATT device, the efficiency is approximately $1/3$ for this case. However, the voltage will be approximately $3/2$ because $\Theta_D = 3\pi/2$ instead of $\pi$ and the capacitance will be lower which is also
Figure 5 Current-Voltage Waveform for a QWITT Device

desirable. It is also seen that the device will exhibit a negative resistance between
\( \omega \tau_D = \pi \) and \( 2\pi \) and thus will not exhibit a negative resistance at low frequencies
which is an important consideration for bias-circuit oscillations.

c. For \( \Theta_m = 3\pi/2 \) (Resonant-Tunneling Injection: QWITT)

\[
\eta = \left( \frac{V_{RF}}{V_{dc}} \right) \sin \frac{\Theta_D}{\Theta_D} .
\]

For \( \Theta_D = \pi/2 \), \( \eta = -\frac{2}{\pi} \frac{V_{RF}}{V_{dc}} \). The current-voltage waveform for this case is shown in
fig. 5.

It is worth noting for this case that if this particular mode of injection is employed,
the negative resistance will exist all the way to d.c. This makes it difficult to stabilize
such devices and spurious oscillations and in particular bias circuit oscillations will be
extremely difficult to suppress. In addition the magnitude of the R.F. voltage swing
for this case will be extremely small and thus the power generation capability will
be very limited. Also depending on the bias point, if the R.F. voltage magnitude
is increased, injection at \( \Theta_m = \pi/2 \) will take place which will be out of phase with
the \( \Theta_m = 3\pi/2 \) case and will decrease the negative resistance and thus the power
output significantly. Therefore, operation of such a device in the transit-time mode
is not desirable and is probably best to minimize transit-time effects and utilize the
inherent negative resistance property. However, the problems of small power output
and spurious oscillations will persist.

d. Ideal case for \( \eta \).

The maximum \( \eta \) is obtained for \( \Theta_w = 0 \), \( \Theta_m = 3\pi/2 \) and \( \Theta_D \approx 0 \). For this
case, \( \eta = -(V_{RF}/V_{dc}) \). The current voltage waveform for this case is shown in fig. 6.
However, the R.F. power generated will be small because \( \Theta_D \) and thus \( V_{dc} \) will be very
small. This does point the way, however, to shape the current-voltage characteristic to optimize $\eta$ if that becomes an important factor.

Since we will be mostly concerned here with TUNNETT devices, fig. 7 shows a heterojunction structure for optimizing the efficiency by inserting spacer layers of GaAlAs. Since $v_s$ in GaAlAs is approximately 1/5 of the saturated velocity in GaAs, the current voltage waveform will be approximately as shown in fig. 7(b), where the induced current during the transit of electrons in the GaAlAs portion of the drift region will be directly proportional to the saturated velocity in this material. This would result in enhanced efficiency [5,7] as shown in fig. 8. It is seen, for example, that for $\beta = 0.2(v_{GaAlAs} = 0.2v_{GaAs})$, the efficiency of a heterojunction-type device can approach that of a conventional IMPATT. Thus, heterojunctions can be employed effectively and in several different configurations to enhance the efficiency and power output of TUNNETT devices. This is an extremely important aspect of recent advances in material growth technology which will aid in improved performance of such devices.

3. TUNNETT Device Design

The basic structure and electric-field profile at the bias point for a basic device are shown in fig. 9. The $i$-layer between the $p^{++}$ and $n^+$ regions is not necessary and can be eliminated. The drift region doping can be designed to optimize performance. This basic structure can operate in several modes depending on the $i$-layer thickness, $x_A$. It has been shown [5] that for a GaAs structure (which will be considered here), if $x_a > 1,000$ Å, $E_c x_A = 1$ and avalanche breakdown occurs and this results in an
Figure 7 Heterojunction TUNNETT Device

Figure 8 Efficiency as a Function of $\delta$ and $\beta$. ($\gamma = 0$)
Figure 9 TUNNET Device

IMPATT device. If \( x_A < 500 \) Å, \( E_c > 10^6 \) V/cm, injection of carriers will be through tunneling and this results in a TUNNETT device. If \( 500 \) Å < \( x_A < 1,000 \) Å, both tunneling and avalanche will be present and this results in a MITTAT device.

It is worth noting here that several means for improving the performance of such two-terminal negative resistance devices exist and such devices have the capability of generating significant amounts of power in the 100–1,000 GHz range. Such basic structures also result in very highly nonlinear capacitance-voltage characteristics before breakdown or tunneling occurs and thus will make excellent varactors for harmonic multiplication particularly when low power levels are available at the fundamental. Such devices do not exhibit an inherent negative resistance at low frequencies (except for rectification effects) and thus would be much easier to stabilize and suppress bias circuit oscillations.

4. Estimation of Expected Power Output From Conventional Single Drift TUNNETT Devices

Since we are interested in a first order estimate of the power generation capability, we will consider here a basic TUNNETT structure. As indicated earlier more complicated structures including hereojunctions and double-drift can be employed to improve performance. From the previous current-voltage waveform (fig. 4) for a TUNNET device \((\Theta_w = 0, \Theta_m = \pi/2 \text{ and } \Theta_D = 3\pi/2)\), the admittance per unit area can be expressed as,

\[
Y_D = -G_D + jB_D
\]
Figure 10 Oscillator Equivalent Circuit

\[
\begin{align*}
Y_d &= \text{the total admittance} \\
&= AY_D = A[-G_D + jB_D] \\
\end{align*}
\]

(9)

where \( A = \text{the area of the device (cm}^2\) \)

\[
\begin{align*}
Z_d &= \text{the total impedance of the device} = -R_d - jX_d \\
&= \frac{1}{Y_D} = \frac{1}{A} \left[ \frac{-G_D}{G_D^2 + B_D^2} - j \frac{B_D}{G_D^2 + B_D^2} \right].
\end{align*}
\]

(10)

The equivalent circuit for an oscillator is shown in fig. 10

where \( R_s = \text{the parasitic diode resistance and circuit loss} \)

\( R_L = \text{the useful load resistance} \)

and \( X_L = \text{the load reactance.} \)
From the oscillation conditions, we have

\[ X_L = X_d ; \quad R_d = R_s + R_L \]

\[ \begin{array}{c}
\bullet \quad 1 \\
A
\end{array}
\left[ \frac{G_D}{G_D^2 + B_D^2} \right] = R_s + R_L \]

and

\[ A = \frac{G_D}{G_D^2 + B_D^2} \frac{1}{R_s + R_L} \quad (12) \]

\[ P_{RF}(Gen.) = \frac{V_{RF}^2}{2} G_d = \frac{V_{RF}^2}{2} (AG_D) \]

\[ = \frac{V_{RF}^2}{2} \left( \frac{G_D^2}{G_D^2 + B_D^2} \right) \frac{1}{R_s + R_L} \quad (13) \]

\[ P_{RF}(R_L) = \text{the power delivered to the load} \]

\[ = P_{RF}(Gen.) \frac{R_L}{R_s + R_L} \]

\[ = \frac{V_{RF}^2}{2} \left( \frac{G_D^2}{G_D^2 + B_D^2} \right) \frac{1}{R_L(1 + R_s/R_L)^2} . \quad (14) \]

For finite \( R_s \), the maximum power delivered to \( R_L \) occurs when \( R_s = R_L \). For this case we have,

\[ P_{RF}(R_L)_{max} = \frac{V_{RF}^2}{2} \left( \frac{G_D^2}{G_D^2 + B_D^2} \right) \frac{1}{4R_L} \quad (15) \]

and

\[ A = \frac{G_D}{G_D^2 + B_D^2} \frac{1}{2R_L} . \quad (16) \]

Next we need to estimate \( V_{RF} \) and \( J_{dc} \). For this we assume the following approximate electric-field profile at the d.c. bias point (as shown in fig. 11).

where

\[ x_A = \text{the effective generation region width} \]
\[ x_D = \text{the drift-region width} \]
\[ E_m = \text{the maximum electric field in the tunneling region} \]
\[ E_D = \text{the field in the drift region} \]
Figure 11 Approximate Electric Field Profile at the d.c. Bias Voltage

and

\[ V_{dc} = (E_m - E_D)x_A + E_D(x_A + x_D). \]  

(17)

If we assume that at \( V_{min} \) (the minimum dynamic voltage at \( \omega t = \frac{3\pi}{2} \)) \( E = E_s \) where \( v \geq v_{sat} \) for \( E \geq E_s \), we find that,

\[ V_{RF} = V_{dc} - V_{min} = E_D(x_A + x_D) - E_S(x_D + x_A) \]  

(18)

and

\[ \frac{V_{RF}}{V_{dc}} = \frac{E_D - E_S}{E_D + (E_m - E_D)\frac{x_A}{x_A + x_D}} \]  

(19)

For the magnitude of current densities which will be encountered \( E_M \approx 1.6 \times 10^6 \text{V/cm} \). With present technology \( x_A = 100 \text{Å} \) can be easily achieved. For TUNNETT devices \( \omega \tau_D = \frac{3\pi}{2} \) and thus

\[ x_D = \frac{3v_s}{4f}. \]  

(20)

It is important to keep carrier generation in the drift region very low. We will therefore assume that

\[ \int_0^{x_D} \alpha \, dx = 0.1 \]  

(21)

where \( \alpha = \text{ionization rate} = Ae^{-(b/E)^m} \).

For GaAs: \( A = 3.85 \times 10^5 \text{cm}^2/\text{V} \cdot \text{cm} \), \( b = 6.85 \times 10^5 \text{V/cm} \) and \( m = 2 \)

\[ A e^{-(b/E_D)^2} x_D = 0.1 \]  

(22)

and

\[ E_D = \frac{b}{\left[ \ln \left( \frac{Ax_D}{0.1} \right) \right]^{1/2}}. \]  

(23)
Assuming $E_s = 3 \times 10^3$ V/cm. and an effective velocity $v_s = 10^7$ cm/sec. we then have the parameters shown in Table I for devices operating at different frequencies.

Next we estimate $J_{dc}$ by considering space charge effects as shown in fig. 12. Assume $\Delta t_{inj} = R_{inj} T$ where $R$ is a constant fraction $= \Theta w/2\pi$. The total charge in the drift region $A J_{max} \Delta t_{inj}$

$$= q A \int_{0}^{z_D} n(x') \, dx'$$

$$\frac{dE_{sc}}{dx} = \rho/\epsilon = \frac{-qn(x)}{\epsilon}$$

$$\Delta E(x) = E(x) - E(o) = \frac{-q}{\epsilon} \int_{0}^{x} n(x') \, dx'$$

$$\Delta E = \Delta E(x_D) = E(x_D) - E(o) = \frac{-q}{\epsilon} \int_{0}^{z_D} n(x') \, dx' = \frac{-q}{\epsilon} \left[ \frac{J_{max} \Delta t_{inj}}{q} \right]$$

$$|\Delta E| = \frac{J_{max} R_{inj} T}{\epsilon} \leq E_D$$

$$J_{DC} = \frac{J_{max} \Delta t_{inj}}{T} = J_{max} R_{inj}$$

$$\bullet\bullet J_{DC} \leq \epsilon E_D f$$

From an estimate of $V_{dc}, V_{RF}$ and $J_{dc}$, the equations given above can be employed in a straightforward manner to estimate the R.F. power which can be expected from such devices.

We will first assume that $R_s + R_L = 1\Omega$, which is unrealistic but serves as a good reference for other more realistic cases. The pertinent parameters for this case are shown in Table II.
Figure 13 Mesa Diode Structure

The series resistance represents power loss and is extremely important for these devices. Figure 13 is a cross-sectional view of a mesa diode. The total positive resistance, $R_s$, associated with the mesa diode is given by [10]

$$ R_s(f) = \frac{\rho_c + \rho_s L_e}{A} + \frac{\rho_s}{\pi \sigma} \left[ 0.5 \ln \frac{b}{d} + h/b \right]. $$

(29)

Where,

- $\rho_c$ is the specific contact resistance in $\Omega \cdot cm^2 (1 \times 10^7)$
- $\rho_s$ is epilayer resistivity in ohms-cm ($\rho_n = 0.00037, \rho_p = 0.0015$)
- $\rho_s$ is the resistivity of the heatsink (gold) in ohms-cm (0.00024)
- $L_e$ is the length of the undepleted epilayers ($L_{n^+} = 0.5 \mu m, L_{p^+} = 0.1 \mu m$)
- $A$ is the area of the diode
- $\sigma$ is the skin depth given by $\sqrt{\frac{2\rho_s}{\mu \omega}}$
- $b$ is the length of the chip (0.02 cm)
- $h$ is the height of the substrate or heatsink (0.005 cm)
- $d$ is the diode diameter.

The series resistance is given in Table III. Taking into account the series resistance, the amount of useful power delivered to $R_L$ is reduced. The results for different diameter devices at the center frequencies of 100, 500 and 1,000 GHz are shown in Tables IV, V and VI respectively.
Another important parameter for cw operation is the thermal resistance which is approximately given by

\[ R_{th} = \frac{2}{\pi K_{hs} d} + \frac{4L}{\pi d^2 K_{sc}} \]  \hspace{1cm} (30)

where,

- \( K_{hs} \) : Thermal conductivity of the heatsink in W/cm °K
  (3.9 for Cu and 11.7 for diamond)
- \( K_{sc} \) : Thermal conductivity of the semiconductor in W/cm °K
  (0.3 for GaAs)
- \( L_{p+} \) : The distance from the junction to the heatsink in cm (0.1 μm)
- \( d \) : is the diode diameter in cm.

The thermal resistance is given in Table VII for different diameters and heat sinks.

From the thermal resistance values given in Table VII, we can estimate the temperature rise in the device for various operating conditions and device diameters. This is done in Table VIII. It can be seen from this table that the diameters chosen for the 100 and 500 GHz operation result in a temperature rise of less than 225°K which is a safe value. However, for 1,000 GHz a diamond heatsink is required to remain below the 225°K temperature rise. Therefore, for this case, \( J_{dc} \) must be reduced for a copper heatsink. For example for a 4 μm-diameter device \( \Delta T = 363°K \). In order to limit \( \Delta T \) to 225°K and maintain the same load impedance, we can reduce \( J_{dc} \) by a factor of 0.62. This will reduce the R.F. power by a factor of 0.38 and thus result in an output power of 2.8 mw which is still significant.

5. Conclusions

Preliminary estimates of the power generation capability of TUNNETT devices in the 100–1,000 GHZ range are promising. It is believed that an output power of 1 mw at one terahertz is feasible.

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REFERENCES


## TABLES

Table I. Important Device Parameters for Different Center Frequencies

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<tr>
<th>f(GHz)</th>
<th>ED(µm)</th>
<th>ED(V/cm)</th>
<th>V_{dc}(V)</th>
<th>V_{RF}(V)</th>
<th>V_{RF}/V_{dc}</th>
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<td>0.75</td>
<td>2.1 x 10^5</td>
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Table II. Estimated $P_{RF}(Gen.)$ and Other Operating Parameters for a 1-Ω Reference $(R_s + R_L = 1Ω)$

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<th>f(GHz)</th>
<th>V_{dc}(V)</th>
<th>V_{RF}(V)</th>
<th>J_{dc}(A/cm^2)</th>
<th>G_D (mhos/cm^2)</th>
<th>B_D (mhos/cm^2)</th>
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Table III. Series Resistance of Mesa Diode

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<td></td>
<td>1.4</td>
<td>2.2</td>
<td>2.7</td>
</tr>
<tr>
<td>5</td>
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<td>1.1</td>
<td>1.8</td>
<td>2.3</td>
</tr>
<tr>
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<td></td>
<td>0.79</td>
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<td>1.9</td>
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<tr>
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<td>0.60</td>
<td>1.2</td>
<td>1.6</td>
</tr>
<tr>
<td>15</td>
<td></td>
<td>0.46</td>
<td>0.96</td>
<td>1.3</td>
</tr>
<tr>
<td>20</td>
<td></td>
<td>0.39</td>
<td>0.84</td>
<td>1.2</td>
</tr>
<tr>
<td>25</td>
<td></td>
<td>0.35</td>
<td>0.75</td>
<td>1.0</td>
</tr>
<tr>
<td>30</td>
<td></td>
<td>0.31</td>
<td>0.68</td>
<td>0.95</td>
</tr>
</tbody>
</table>

Table IV. Estimated Power Output Including \( R_s \)

\[ f = 100 \text{ GHz} \]

\[ J_{dc} = 22.3 \times 10^3 \text{ A/cm}^2; \ V_{dc} = 17.4V; \ V_{RF} = 15.7V \]

<table>
<thead>
<tr>
<th>Diode Diam. (µm)</th>
<th>Area (cm(^2))</th>
<th>( R_s (Ω) )</th>
<th>(-R_d(Ω))</th>
<th>( R_L(Ω) )</th>
<th>( I_{dc} (mA) )</th>
<th>( P_{dc} (w) )</th>
<th>( P_{RF} ) (Gen.) (mw)</th>
<th>( P_{RL} ) (RL) (mw)</th>
<th>( \eta % )</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>2.9 \times 10^{-6}\</td>
<td>0.39</td>
<td>3</td>
<td>2.61</td>
<td>66</td>
<td>1.15</td>
<td>217</td>
<td>189</td>
<td>16.4</td>
</tr>
<tr>
<td>25</td>
<td>4.5 \times 10^{-6}\</td>
<td>0.35</td>
<td>2.4</td>
<td>2</td>
<td>100</td>
<td>1.75</td>
<td>271</td>
<td>225</td>
<td>13</td>
</tr>
<tr>
<td>30</td>
<td>6.5 \times 10^{-6}\</td>
<td>0.31</td>
<td>2</td>
<td>1.69</td>
<td>145</td>
<td>2.52</td>
<td>325</td>
<td>275</td>
<td>11</td>
</tr>
<tr>
<td>30</td>
<td>6.5 \times 10^{-6}\</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>145</td>
<td>2.52</td>
<td>325</td>
<td>162</td>
<td>6.4</td>
</tr>
</tbody>
</table>
Table V. Estimated Power Output Including \( R_s \),
\[ f = 500 \text{ GHz} \]
\[ J_{dc} = 2.2 \times 10^5 \text{A/cm}^2; \ V_{dc} = 7.8V; \ V_{RF} = 6.5V \]

<table>
<thead>
<tr>
<th>Diode Diam. (( \mu \text{m} ))</th>
<th>Area (cm(^{-2} ))</th>
<th>( R_s (\Omega) )</th>
<th>(-R_d (\Omega) )</th>
<th>( R_L (\Omega) )</th>
<th>( I_{dc} (\text{ma}) )</th>
<th>( P_{dc} (\text{mw}) )</th>
<th>( P_{RF} (\text{Gen.}) (\text{mw}) )</th>
<th>( P_{RL} (\text{R}_L) (\text{mw}) )</th>
<th>( \eta % )</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>( 1.16 \times 10^{-7} )</td>
<td>2.2</td>
<td>3.36</td>
<td>1.16</td>
<td>25.5</td>
<td>200</td>
<td>35</td>
<td>12</td>
<td>6</td>
</tr>
<tr>
<td>5</td>
<td>( 1.8 \times 10^{-7} )</td>
<td>1.8</td>
<td>2.16</td>
<td>0.36</td>
<td>39.6</td>
<td>309</td>
<td>55</td>
<td>9.2</td>
<td>3</td>
</tr>
<tr>
<td>7</td>
<td>( 3.9 \times 10^{-7} )</td>
<td>1.4</td>
<td>1</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
</tr>
</tbody>
</table>

will operate at a lower \( V_{RF} \)

<table>
<thead>
<tr>
<th>Diode Diam. (( \mu \text{m} ))</th>
<th>Area (cm(^{-2} ))</th>
<th>( R_s (\Omega) )</th>
<th>( R_L (\Omega) )</th>
<th>( -R_d (\Omega) )</th>
<th>( V_{RF} (\text{V}) )</th>
<th>( I_{dc} (\text{ma}) )</th>
<th>( P_{dc} (\text{mw}) )</th>
<th>( P_{RF} (\text{Gen.}) (\text{mw}) )</th>
<th>( P_{RL} (\text{R}_L) (\text{mw}) )</th>
<th>( \eta % )</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>( 1.16 \times 10^{-7} )</td>
<td>2.2</td>
<td>2.2</td>
<td>4.4</td>
<td>4.96</td>
<td>25.5</td>
<td>200</td>
<td>27</td>
<td>13.5</td>
<td>6.75</td>
</tr>
<tr>
<td>5</td>
<td>( 1.8 \times 10^{-7} )</td>
<td>1.8</td>
<td>1.8</td>
<td>3.6</td>
<td>3.9</td>
<td>39.6</td>
<td>309</td>
<td>33</td>
<td>16.5</td>
<td>5.3</td>
</tr>
<tr>
<td>7</td>
<td>( 3.9 \times 10^{-7} )</td>
<td>1.4</td>
<td>1.4</td>
<td>2.8</td>
<td>2.32</td>
<td>86</td>
<td>670</td>
<td>42.3</td>
<td>21</td>
<td>3</td>
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<tr>
<td>10</td>
<td>( 7.2 \times 10^{-7} )</td>
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<td>1.2</td>
<td>2.4</td>
<td>1.46</td>
<td>158.4</td>
<td>1,235</td>
<td>49</td>
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</table>
Table VI. Estimated Power Output Including $R_s$

\[ f = 1000 \text{ GHz} \]

\[ J_{dc} = 7 \times 10^5 \text{ A/cm}^2; \quad V_{dc} = 6.6 \text{ V} \]

(Because of series resistance, the device cannot oscillate at $V_{RF} = 5.5 \text{ V}$s where maximum $\eta$ is obtained, but will oscillate at a lower $V_{RF}$)

<table>
<thead>
<tr>
<th>Diode Diam. ($\mu$m)</th>
<th>Area (cm$^{-2}$)</th>
<th>$R_s$ (Ω)</th>
<th>$R_L$ (Ω)</th>
<th>$-R_d$ (Ω)</th>
<th>$V_{RF}$ (V)</th>
<th>$I_{dc}$ (mA)</th>
<th>$P_{dc}$ (w)</th>
<th>$P_{RF}$ (Gen.) (mw)</th>
<th>$P_{RL}$ (RL) (mw)</th>
<th>$\eta$%</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>$1.16 \times 10^{-7}$</td>
<td>2.7</td>
<td>2.7</td>
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<td>15</td>
<td>7.5</td>
<td>1.4</td>
</tr>
<tr>
<td>5</td>
<td>$1.8 \times 10^{-7}$</td>
<td>2.3</td>
<td>2.3</td>
<td>4.6</td>
<td>0.66</td>
<td>126</td>
<td>832</td>
<td>17.6</td>
<td>8.8</td>
<td>1</td>
</tr>
<tr>
<td>7</td>
<td>$3.9 \times 10^{-7}$</td>
<td>1.9</td>
<td>1.9</td>
<td>3.8</td>
<td>3.7</td>
<td>273</td>
<td>1,800</td>
<td>21</td>
<td>10.5</td>
<td>.5</td>
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</table>

Table VII. Thermal Resistance of a Mesa Diode

<table>
<thead>
<tr>
<th>Diameter ($\mu$m)</th>
<th>$R_{th} =$ Diode Thermal Resistance ($10^2 \text{ °K/W}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Copper heatsink</td>
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<tr>
<td>1</td>
<td>58.7</td>
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<td>2</td>
<td>18.8</td>
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<td>10</td>
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<td>15</td>
<td>1.28</td>
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<tr>
<td>20</td>
<td>0.92</td>
</tr>
<tr>
<td>25</td>
<td>0.72</td>
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<tr>
<td>30</td>
<td>0.59</td>
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</table>
Table VIII. Estimated CW Power

<table>
<thead>
<tr>
<th>f(GHz)</th>
<th>Diode Diam. (μm)</th>
<th>$P_{dc}(w)$</th>
<th>$R_{th}(°/w)$ Cu</th>
<th>$R_{th}(°/w)$ Diamond</th>
<th>$ΔT(°K)$ Cu</th>
<th>$ΔT(°K)$ Diamond</th>
<th>$P_{RF}(mw)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>20</td>
<td>1.15</td>
<td>92</td>
<td>106</td>
<td>48</td>
<td>189</td>
<td></td>
</tr>
<tr>
<td></td>
<td>25</td>
<td>1.75</td>
<td>72</td>
<td>126</td>
<td>51</td>
<td>225</td>
<td></td>
</tr>
<tr>
<td></td>
<td>30</td>
<td>2.52</td>
<td>59</td>
<td>150</td>
<td>58</td>
<td>275</td>
<td></td>
</tr>
<tr>
<td>500</td>
<td>5</td>
<td>0.31</td>
<td>496</td>
<td>154</td>
<td>86</td>
<td>16.5</td>
<td></td>
</tr>
<tr>
<td></td>
<td>7</td>
<td>0.67</td>
<td>320</td>
<td>214</td>
<td>110</td>
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<td></td>
</tr>
<tr>
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<tr>
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<td>576</td>
<td>295</td>
<td>10.5</td>
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